

# Ch2 - Ex1 - Age and Memory

DATA LIST FREE / age mem.

BEGIN DATA

1 36 1 32 1 29 1 31 1 28 1 34 1 32 1 27 1 34 1 30 1 26 1 31  
 2 26 2 30 2 28 2 31 2 31 2 24 2 27 2 29 2 32 2 26 2 30 2 25

END DATA.

\*On average, younger adults remember 32 words on this task. Do results suggest that this sample comes from a population that remembers more or fewer words.

TTTEST TESTVALUE = 32 / VARI = mem.

	N	Mean	Std. Deviation	Std. Error Mean
mem	24	29.54167	3.064228	.625483

t	df	Test Value = 32 Sig. (2-tailed)	Mean Difference	
mem	-3.930	23	.001	-2.458333

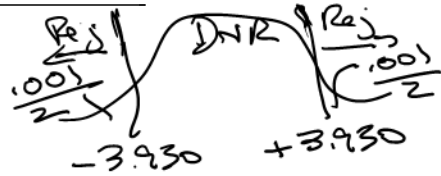
$H_0: \mu = 32$   
 $H_a: \mu \neq 32$

$$t = \frac{\bar{Y} - \mu_0}{s/\sqrt{n}}$$

$$= \frac{29.54167 - 32}{.6255} = -3.930$$

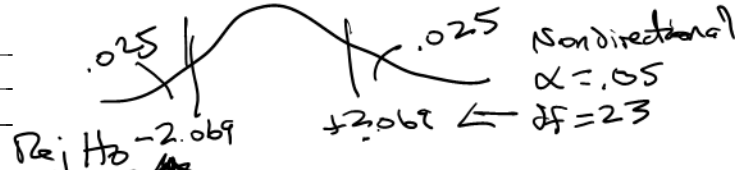
COMPUTE mem32 = mem-32.  
 GLM mem32 /PRINT = DESCR.

$\alpha = .05$   
 Rej  $H_0$   
 Acc  $H_0$



Dependent Variable: mem32

Mean	Std. Deviation	N
-2.45833	3.064228	24



Dependent Variable: mem32

Source	Type III Sum of Squares	df	Mean Square	F	Sig.
Corrected Model	.000	0	.	.	.
Intercept	145.042	1	145.042	15.45	.001
Error	215.958	23	9.389		
Total	361.000	24			
Corrected Total	215.958	23			

$n \times (\bar{Y} - \mu_0)^2$   
 $24 \times (-2.4583)^2 = 145.038$

$F = \frac{MS_{Intercept}}{MS_{Error}} = \frac{145.042}{9.389} = 15.45$

$t^2 = F$

\*Sampling Distribution: 100,000 samples, mu = 32, sigma = 5, n = 24.

SET SEED = 14222318.

INPUT PROGRAM.

LOOP sample = 1 TO 100000.

DO REPEAT y = y1 TO y24.

COMPUTE #a = RV.NORM(0,1).

COMPUTE y = 32+5\*(-.707107\*#a + .707107\*RV.NORM(0,1)).

$\sqrt{F} = 3.93 = t$   
 $t^2 = F$

$df = 23$   
 $F_{\alpha} = 4.28 = 2.069^2 = t_{\alpha}^2$

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END REPEAT.
END CASE.
END LOOP.
END FILE.
END INPUT PROGRAM.

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COMPUTE mean = MEAN(y1 TO y24).
COMPUTE variance = SD(y1 TO y24)**2.
COMPUTE t = (mean-32)/SQRT(variance/24).
COMPUTE pobs = ABS(t) GE 3.930297.
COMPUTE palpha = ABS(t) GE 2.069.
MEANS pobs palpha.

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$$t = \frac{\bar{y} - \mu_0}{s/\sqrt{n}}$$

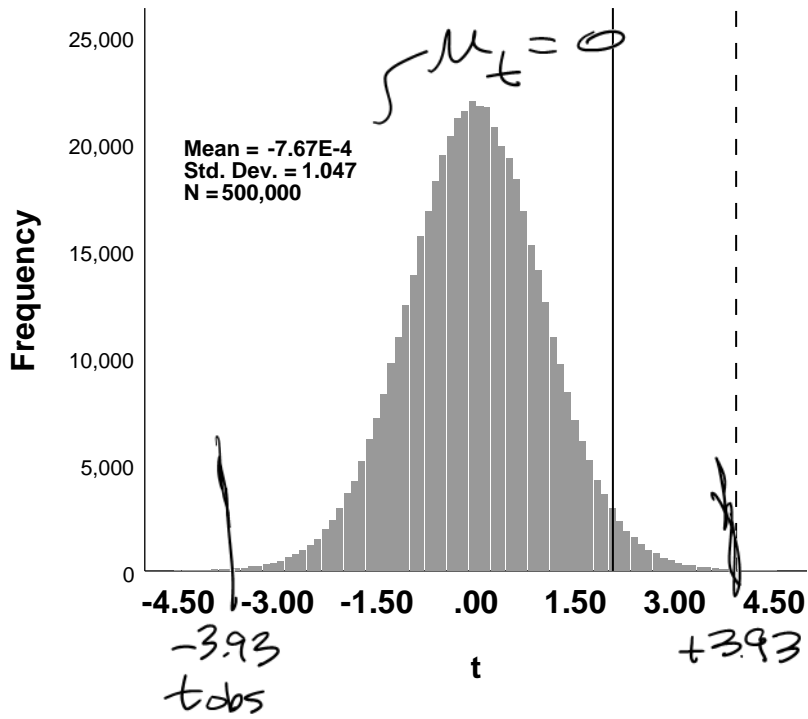
$\sim \leq -3.93$  OR  $\geq +3.93$

	pobs	palpha
Mean	.00073	.04863

$p = \frac{73}{100,000} = .0007$

our t-test  
 $p = .001 = .00066$

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FREQ t /FORM = NOTABLE /HISTOGRAM.
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\*Independent groups.

TTEST VARI = mem /GROUP = age.

	age	N	Mean	Std. Deviation
mem	1.000 Young	12	30.83333	3.010084
	2.000 Old	12	28.25000	2.632835

$$SS_1 = (11-1)3.01008^2$$

$$s_p^2 = \frac{2 SS_1 + 2 SS_2}{df_1 + df_2} = 7.9962$$

$$SS_2 = (11-1)2.63283^2$$

t-test for Equality of Means					
	t	df	Sig. (2-tailed)	Mean Difference	Std. Error Difference
mem	2.238	22	.036	2.583333	1.154427

$$s_p^2 \left( \frac{1}{n_1} + \frac{1}{n_2} \right)$$

$H_0: \mu_1 = \mu_2$   
 $H_a: \mu_1 > \mu_2$

$$t_{obs} = \frac{(\bar{y}_1 - \bar{y}_2) - 0}{\sqrt{s_p^2 \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

GLM mem BY age /PRINT = DESCR.

Dependent Variable: mem

age	Mean $\bar{y}_j$	Std. Deviation	N
1.000 $\bar{y}_1$	30.83333	3.010084	12
2.000 $\bar{y}_2$	28.25000	2.632835	12
Total $\bar{y}_G$	29.54167	3.064228	24

$$\bar{y}_j - \bar{y}_G$$

$$1.292$$

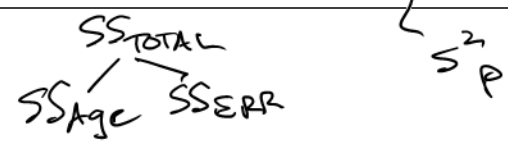
$$-1.292$$

$$12 \times \Sigma^2 = 40.042$$

Dependent Variable: mem

Source	Type III Sum of Squares	df	Mean Square	F	Sig.
age	40.042	1	40.042	5.008	.036
Error	175.917	22	7.996		
Corrected Total	215.958	23			

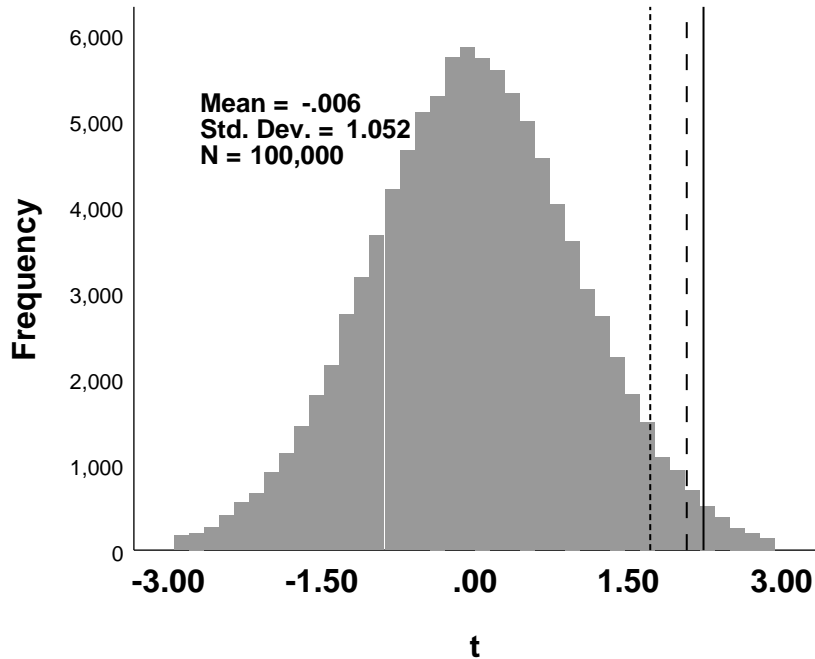
$$= F_t$$



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*Simulation H0 true: mu1 = mu2.
SET SEED = 14222318.
INPUT PROGRAM.
LOOP sample = 1 TO 100000.
DO REPEAT y = y1 TO y12.
  COMPUTE y = 32+5*RV.NORM(0,1).
END REPEAT.
DO REPEAT o = o1 TO o12.
  COMPUTE o = 32+5*RV.NORM(0,1).
END REPEAT.
END CASE.
END LOOP.
END FILE.
END INPUT PROGRAM.
COMPUTE diff = MEAN(y1 TO y12) - MEAN(o1 TO o12).
COMPUTE var = (SD(y1 TO y12)**2 + SD(o1 TO o12)**2)/2.
COMPUTE t = diff/SQRT(var*(1/12 + 1/12)).

FREQ t /FORMAT = NOTABLE /HIST.
  
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COMPUTE pobsnnon = ABS(t) GE 2.238.
COMPUTE pobsdir = t GE 2.238.
COMPUTE palphanon = ABS(t) GE 2.074.
COMPUTE palphadir = t GE 1.717.
MEANS pobsnnon pobsdir palphanon palphadir.

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$H_a: \mu_1 \neq \mu_2$   
 $H_a: \mu_1 > \mu_2$

	pobsnnon	pobsdir	palphanon	palphadir
Mean	.03564	.01735	.05030	.04984

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*SPSS commands to generate sample data.
SET SEED = 14222318.
INPUT PROGRAM.
LOOP #s = 1 TO 24.
END CASE.
END LOOP.
END FILE.
END INPUT PROGRAM.
COMPUTE #a = RV.NORM(0,1).
COMPUTE yrs = RND(55+10*#a).
COMPUTE mem = RND(30+5*(-.7071*#a + .7071*RV.NORM(0,1))).
SORT CASES BY yrs.
RANK yrs /NTILE(2) INTO age.
FORMAT mem yrs (F2.0) age (F1.0).
DELETE VARI yrs.
LIST age mem.

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